

Supplementary notes

^{133}Ba ($\tau_{1/2} \approx 10.5\text{yr}$) is manufactured via neutron activation of ^{132}Ba . A 1 mCi sample purchased from Eckert & Ziegler contained an estimated isotopic content of a few percent ^{133}Ba and the remainder primarily ^{132}Ba .

493 nm	$(V_{493}^c, V_{493}^{sb})$	$(V_{493}^c, V_{493}^{op})$		$(V_{493}^c, V_{493}^{sb})$	$(V_{493}^c, V_{493}^{sb})$	$(V_{493}^c, V_{493}^{sb})$	$(V_{493}^c, V_{493}^{op})$		$(V_{493}^c, V_{493}^{sb})$	$(V_{493}^c, V_{493}^{sb})$	
650 nm	$(V_{650}^c, V_{650}^{sb})$	$(V_{650}^c, V_{650}^{sb})$	V_{650}^c	$(V_{650}^c, V_{650}^{sb})$	$(V_{650}^c, V_{650}^{sb})$	$(V_{650}^c, V_{650}^{sb})$	$(V_{650}^c, V_{650}^{sb})$		V_{650}^c	$(V_{650}^c, V_{650}^{sb})$	$(V_{650}^c, V_{650}^{sb})$
455 nm			V_{455}						V_{455}		
585 nm			V_{585}						V_{585}		
614 nm				V_{614}						V_{614}	
3.02 cm	(a)					(b)					Δ_1
	Doppler Cooling t = 4.5 ms	$ 0\rangle$ Prep t = 100 μs	Shelving t = 300 μs	State Detection t = 4.5 ms	Deshelving t = 1.0 ms	Doppler Cooling t = 4.5 ms	$ 1\rangle$ Prep t = 150 μs	Shelving t = 300 μs	State Detection t = 4.5 ms	Deshelving t = 1.0 ms	
493 nm	$(V_{493}^c, V_{493}^{sb})$			$(V_{493}^c, V_{493}^{sb})$	$(V_{493}^c, V_{493}^{sb})$	$(V_{493}^c, V_{493}^{sb})$	$(V_{493}^c, V_{493}^{sb})$		$(V_{493}^c, V_{493}^{sb})$	$(V_{493}^c, V_{493}^{sb})$	
650 nm	$(V_{650}^c, V_{650}^{sb})$	$(V_{650}^c, V_{650}^{sb})$		$(V_{650}^c, V_{650}^{sb})$	$(V_{650}^c, V_{650}^{sb})$	$(V_{650}^c, V_{650}^{sb})$	$(V_{650}^c, V_{650}^{sb})$		$(V_{650}^c, V_{650}^{sb})$	$(V_{650}^c, V_{650}^{sb})$	
455 nm			V_{455}				V_{455}				
585 nm											
614 nm				V_{614}					V_{614}	V_{614}	
	(c)					(d)					
	Doppler Cooling t = 4.5 ms	$ S_{1/2}, F=1\rangle$ Prep t = 100 μs	455 nm scan t = 50 μs	State Detection t = 4.5 ms	Deshelving t = 1.0 ms	Doppler Cooling t = 4.5 ms	$(D_{5/2})$ Prep t = 300 μs	614 nm scan t = 100 μs	State Detection t = 4.5 ms	Deshelving t = 1.0 ms	

Supplementary Figure 1. Experimental sequences for hyperfine qubit SPAM and $^{133}\text{Ba}^+$ spectroscopy. (a) SPAM sequence of $|0\rangle$ state. All lasers are linearly polarized $\approx 45^\circ$ from the magnetic field direction except v_{455} , linearly polarized along the magnetic field (π -light). (b) SPAM of the $|1\rangle$ state is identical to SPAM of the $|0\rangle$ state with the addition of microwaves near 9.925 GHz after $|0\rangle$ state initialization. (c) Sequence for measuring $^2P_{3/2}$ hyperfine splitting and $^2P_{3/2} \leftrightarrow ^2S_{1/2}$ isotope shift. (d) Sequence for measuring $^2D_{5/2}$ hyperfine splitting and $^2P_{3/2} \leftrightarrow ^2D_{5/2}$ isotope shift.

References

1. Hucul, D., Christensen, J. E., Hudson, E. R. & Campbell, W. C. Spectroscopy of a synthetic trapped ion qubit. *Phys. Rev. Lett.* **119**, 100501 (2017).
2. Knab, H., Schupp, M. & Werth, G. Precision spectroscopy on trapped radioactive ions: Ground-state hyperfine splittings of $^{133}\text{Ba}^+$ and $^{131}\text{Ba}^+$. *Eur. Lett.* **4**, 1361 (1987).
3. Höhle, C., Hühnermann, H., Meier, T., Ihle, H. & Wagner, R. Nuclear moments and optical isotope shift of radioactive ^{133}Ba . *Phys. Lett. B* **62**, 390 – 392 (1976).

Supplementary Table 1. $^{133}\text{Ba}^+$ hyperfine splittings and isotope shifts relative to $^{138}\text{Ba}^+$. For reported isotope shifts of the i -th electronic transition, defined as $\delta\nu^i \equiv \nu_{133}^i - \nu_{138}^i$, centroid frequencies (ν_{133}^i) are calculated from hyperfine measurements and compared to corresponding transitions in $^{138}\text{Ba}^+$. Bolded values are measurements from this work. $\delta\nu^{585}$ is calculated using previous measurements¹ and results from this work. Hyperfine splittings include a 20 MHz systematic uncertainty due to unresolved Zeeman structure. Isotope shifts include a 28 MHz systematic uncertainty due to unresolved Zeeman structure and wavemeter drift.

Hyperfine Splitting	Frequency (MHz)
$^2\text{S}_{1/2}$	9925.45355459(10) ²
$^2\text{P}_{1/2}$	1810(11) ³
$^2\text{P}_{3/2}$	623 (20)
$^2\text{D}_{3/2}$	937 (20) ¹
$^2\text{D}_{5/2}$	83 (20)
Isotope Shift	Frequency (MHz)
$\delta\nu^{493}$	373(4) ³
$\delta\nu^{455}$	358(28)
$\delta\nu^{650}$	198(20) ¹
$\delta\nu^{614}$	216(28)
$\delta\nu^{585}$	183(35)